Dielectric Relaxation of NaClO₄ Solutions in Formamide, N-Methylformamide, and N,N-Dimethylformamide

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Dedicated to Prof. Hitoshi Ohtaki on the occasion of his 60th birthday

Complex permittivity spectra in the frequency range 0.95 ≤ ν/[GHz] ≤ 89 for N,N-dimethylformamide (DMF), N-methylformamide (NMF), formamide (FA) and their solutions of NaClO₄ are investigated to study the change of liquid structure and dynamics arising from the availability of one hydrogen-bond acceptor site together with no (DMF), one (NMF), or two (FA) donor sites on the same molecule. Three solvent relaxation processes are observed for NMF and two for FA and DMF. The relaxation parameters are used to determine solvation numbers. They show that ion-solvent interactions lead to a reduction of the average length of the H-bonded NMF chains but have only moderate influence on the FA structure. An additional solute relaxation process in DMF solutions is due to the diffusion-controlled formation and decomposition of solvent-shared ion pairs.

Key words: Dielectric relaxation, Formamides, Solvation, Solvent dynamics, Ion association.

1. Introduction

Due to high polarity and strong solvating power combined with a large liquid state range, formamide (FA) as well as its derivatives N-methylformamide (NMF) and N,N-dimethylformamide (DMF) are interesting solvents in research and technical processes [1, 2, 3]. In addition, NMF is the simplest molecule incorporating the biologically important O=C–NHR configuration characteristic for peptides. Therefore the solution properties of the amides have extensively been studied, see [4, 5]. Diffraction experiments [6, 7, 8, 9, 10] reveal the impact of hydrogen bonding on the structure of the neat liquids ranging from the random distribution of molecular dipole orientations in DMF via the formation of flexible chains with preferred parallel orientation of the molecular moments μ, in NMF to the three-dimensional arrangement of FA molecules, where the formation of ring-dimers reduces the macroscopic dipole moment M = Σμ, compared to NMF.

Much less is known about the dynamics of the amides, especially the cooperative processes arising from hydrogen bonding, and on the structural implications of ion solvation. Such processes can be successfully investigated by dielectric relaxation studies [11, 12] provided the complex permittivity spectra

\[ \varepsilon(\omega) = \varepsilon'(\omega) - i\varepsilon''(\omega), \quad \omega = 2\pi\nu, \]

are recorded with high accuracy over a wide range of frequencies ν, a requirement only incompletely met by the older dielectric studies of electrolyte solutions in the formamides [13, 14, 15]. The frequency dependence of the complex permittivity, ε(ω), probes the individual contributions to the relaxation of the sample polarization P(t) after a change of the applied electrical field provided their relaxation times τ are sufficiently different. In electrolyte solutions these processes may arise from the reorientation of individual solvent dipoles, from the kinetics of ion-pair formation, and from structural relaxation of the H-bonded aggregates. Fast intramolecular contributions due to molecular polarizability are outside the observation window of interest and are subsumed in the “infinite frequency” permittivity εₓₓ.

In this contribution we present results from complex permittivity measurements in the frequency range 0.95 ≤ ν/[GHz] ≤ 89 for solutions of NaClO₄ in FA, NMF, and DMF at 25°C, supplementing the preliminary report on the dielectric properties of the neat solvents [16].

2. Experimental

2.1. Materials

The solvents formamide (Merck p.A.), N-methylformamide (Fluka purum), and N,N-dimethylform-
amide (Fluka p.A.) were dried over molecular sieve (FA: Merck 0.3 nm; DMF, NMF: Merck 0.4 nm) for at least 7 days and then fractionally distilled under reduced pressure (≤ 2 Torr) using a closed apparatus with two packed columns in line [17]. Gaschromatographically determined organic impurities amounted to less than 0.08% for all batches used in the experiments, residual water in FA < 130 ppm, in NMF < 150 ppm, and in DMF < 100 ppm. Column 3 of Table 1 reports the maximum conductivity of the purified solvents. To monitor eventual solvent decomposition during the measurements, the data refer to purity checks performed after all experiments, i.e. 4–5 weeks after distillation.

NaClO₄ (Merck p.A.) was recrystallized twice from water and vacuumdried at 140 °C over Sicapent® (Merck) for 7 days. Sample preparation by weight and experiments were carried out under an atmosphere of dry nitrogen.

2.2. Measurements

Complex permittivities of the solutions at 25.00 ± 0.01 °C were determined at 28 to 31 frequencies with the help of one coaxial (0.95 to 2.5 GHz) and five waveguide devices (4 to 89 GHz) using the method of travelling waves. Details of the equipment are given in [18,19]. The determined wavelengths λ_M(v) and attenuation coefficients α(v) directly yield the complex generalised permittivity

\[ \tilde{\varepsilon}(\omega) = \varepsilon' - i\frac{\varepsilon''(\omega)}{\varepsilon_0} \]

comprising dielectric displacement and ohmic contribution of the sample response; ε₀ is the permittivity of the vacuum. At ν < 40 GHz a precision of 1.5% for the real part of \( \tilde{\varepsilon}(\omega) \) and of 2.5% for the imaginary part is achieved; at higher frequencies we have 3% for \( \varepsilon' \) and \( \varepsilon'' \).

To obtain the complex permittivity \( \tilde{\varepsilon}(\omega) \) from (1), the common assumption is made that \( \varepsilon''(\omega) \) equals the real part \( \varepsilon(0) = \varepsilon \) obtained at quasi-static frequencies (ν → 0). These conductivity data were determined with a precision of 0.1% using standard methods of our laboratory [17]. Densities \( \varrho \) for the conversion of solute molalities to molar concentrations \( c \) were obtained with a vibrating-tube density meter (Paar DMA60/DMA602) using air and degassed water as the references. Viscosities \( \eta \) were determined with the help of an Ubbelohde viscometer with optoelectronic detection (Schott AVS/G) using water as the reference. The results for \( \varrho, \varepsilon \) and \( \eta \) are summarized in Table I.

<table>
<thead>
<tr>
<th>c</th>
<th>( \varrho )</th>
<th>( \varepsilon )</th>
<th>( \eta )</th>
</tr>
</thead>
<tbody>
<tr>
<td>mol dm⁻³</td>
<td>kg m⁻³</td>
<td>\Omega⁻¹ m⁻¹</td>
<td>10⁻³ Pa s</td>
</tr>
<tr>
<td>FA</td>
<td></td>
<td></td>
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<tr>
<td>0.14256</td>
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<td>0.52637</td>
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<tr>
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<td>1.73</td>
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<td>0.858</td>
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<td>2.4735</td>
<td>1.90</td>
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3. Results and Discussion

3.1. Relaxation Models

The formal description of the complex permittivity spectra was achieved by fitting a semi-empirical relaxation model expressed as the sum of Havriliak-Negami type processes

\[ \tilde{\varepsilon}(\omega) = \varepsilon_\infty + (\varepsilon - \varepsilon_\infty) \sum_{j=1}^{n} \frac{g_j}{[1 + (i\omega\tau_j)^{\gamma_j}]} \]

comprising \( n \) discernable relaxation processes \( j \) of relaxation time \( \tau_j \) and weight \( g_j \)

\[ g_j = \frac{\varepsilon_j - \varepsilon_\infty}{\varepsilon - \varepsilon_\infty} \]

\[ \varepsilon_1 = \varepsilon_\infty + \varepsilon_j \]

\[ \varepsilon_{j+1} = \varepsilon_{j+1} \]

\[ \varepsilon_{n\infty} = \varepsilon_\infty \]

with the special cases \( \chi_j = 0, 0 < \beta_j < 1 \) (Davidson-Cole process), \( 0 < \chi_j < 1, \beta_j = 1 \) (Cole-Cole process), and \( \chi_j = 0, \beta_j = 1 \) (Debye process). \( \varepsilon = \varepsilon'(0) \) is the static permittivity of the solution. Figure 1 shows a typical example for the investigated solutions and defines the more informative notation subsequently used in the text, where the index \( s \) designates that the parameter originates from a relaxation process of the solvent and \( IP \) represents the solute.

When only data up to 89 GHz are considered, the normalized sum of squared residuals, \( \chi^2 \), does not allow to discriminate between several possible models for the neat solvents [16]. Inclusion of far-infrared
Fig. 1. Complex permittivity spectrum of a 1.02 mol dm$^{-3}$ solution of NaClO$_4$ in DMF at 25°C. a) Frequency dependence of dielectric dispersion and loss, $\varepsilon'(v)$ resp. $\varepsilon''(v)$, and of the total loss $\eta''(v) = \varepsilon'' + \varepsilon_0/\varepsilon_\infty$; b) the corresponding Argand diagrams. The shaded areas represent the individual contributions of the ion-pair (IP) and of the solvent relaxation processes $s1$ and $s2$.

(FIR) data in the range $234 \leq v/\text{GHz} \leq 293$ for DMF [20] and $146 \leq v/\text{GHz} < 293$ for NMF [21] yields an unambiguous decision. The relaxation of DMF is governed by two Debye processes of parameters $\varepsilon_s = 37.25$, $\tau_{s1} = 10.36$ ps, $\varepsilon_{s2} = 4.41$, $\tau_{s2} = 0.74$ ps, $\varepsilon_\infty = 2.84$. The slightly different set of parameters compared to [16] results from a re-determination of $\varepsilon(\omega)$ in the 13 to 17.5 GHz region with improved cell design and from more precise far-infrared data compared to [22]. For NMF three Debye processes are found with parameters $\varepsilon_s = 183.3$, $\tau_{s1} = 127.6$ ps, $\varepsilon_{s2} = 6.13$, $\tau_{s2} = 7.9$ ps, $\varepsilon_{s3} = 4.60$, $\tau_{s3} = 0.79$ ps, $\varepsilon_\infty = 3.20$.

It might be argued that fitting a Debye process of $\tau \approx 0.8$ ps to complex permittivity spectra of asymmetric rotors with large moments of inertia is questionable. Indeed, the experimental FIR spectrum of DMF exhibits a considerable half width of the libration band centered around 70 cm$^{-1}$ (2000 GHz) which distinctly exceeds the result obtained from the Gaussian-cage model [20], and NMF exhibits a strong absorption ($\varepsilon_{\text{max}} = 695 \text{ Np cm}^{-1}$ at 116 cm$^{-1}$) with a large low-frequency tail [21]. However, for the electrolyte solutions only the assumption of two Debye processes for the solvent relaxation of DMF and of three processes for NMF yields consistent results with a minimum scatter of the obtained relaxation parameters as functions of electrolyte concentration $c$, and allows the interpretation of the results in terms of physical processes. This argument also allows to select the combination of a slow Cole-Cole and a fast Debye process as most appropriate for FA and its NaClO$_4$ solutions (parameters at $c = 0$: $\varepsilon_s = 108.8$, $\tau_{s1} = 37.32$ ps, $\varepsilon_{s2} = 0.006$, $\varepsilon_{s3} = 7.08$, $\tau_{s3} = 1.2$ ps, $\varepsilon_\infty = 4.48$). An additional low-frequency Debye dispersion, parameters $\varepsilon_s$, $\tau_{s1}$, $\varepsilon_{\text{ip}}$, arises at increasing electrolyte concentrations for DMF solutions due to ion-pair (IP) formation. Tables 2–4 summarize the results and the corresponding $\chi^2$. To reduce the number of adjustable parameters for the electrolyte solutions covering $v \leq 89$ GHz the permittivities $\varepsilon_\infty$ were fixed to the corresponding values of the neat solvents for NMF (Table 3) and DMF (Table 4). The error margins given in Tables 2–4 are the maximum deviations from appropriate polynomial fits to the $\varepsilon_j$ and $\tau_j$ vs. $c$. These quantities yield a more reasonable estimate of the precision than the relative uncertainties of the parameters from non-linear least squares routines.
Table 2. Relaxation parameters of NaClO₄ solutions in formamide at 25 °C.

<table>
<thead>
<tr>
<th>c (mol dm⁻³)</th>
<th>ε = εₛ</th>
<th>τₛ₁ (ps)</th>
<th>xₛ₁</th>
<th>εₛ₂</th>
<th>τₛ₂ (ps)</th>
<th>εₐ∞</th>
<th>χ²</th>
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<tbody>
<tr>
<td>±0.5</td>
<td>±0.04</td>
<td>±0.004</td>
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<td>37.60</td>
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<td>94.9</td>
<td>37.89</td>
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<td>7.34</td>
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<td>86.7</td>
<td>38.66</td>
<td>0.023</td>
<td>7.77</td>
<td>1.8</td>
<td>5.3</td>
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Table 3. Relaxation parameters of NaClO₄ solutions in N-methylformamide at 25 °C.

<table>
<thead>
<tr>
<th>c (mol dm⁻³)</th>
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<th>εₛ₂</th>
<th>τₛ₂ (ps)</th>
<th>εₛ₃</th>
<th>τₛ₃ (ps)</th>
<th>εₐ∞</th>
<th>χ²</th>
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<td>±0.08</td>
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<td>±0.07</td>
<td>±0.1</td>
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<tr>
<td>0.0</td>
<td>183.3</td>
<td>127.6</td>
<td>6.13</td>
<td>7.9</td>
<td>4.60</td>
<td>0.79</td>
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<td>0.36</td>
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<tr>
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<td>169.2</td>
<td>123.9</td>
<td>6.32</td>
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<td>4.56</td>
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<td>3.20</td>
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<td>0.8</td>
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<tr>
<td>0.89030</td>
<td>93.3</td>
<td>99.4</td>
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<td>0.8</td>
<td>3.20</td>
<td>0.18</td>
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Table 4. Relaxation parameters of NaClO₄ solutions in N,N-dimethylformamide at 25 °C.

<table>
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<tr>
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<th>τₛ₁ (ps)</th>
<th>εₛ₂</th>
<th>τₛ₂ (ps)</th>
<th>εₛ₃</th>
<th>τₛ₃ (ps)</th>
<th>εₐ∞</th>
<th>χ²</th>
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<td>±0.1</td>
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<td>—</td>
<td>37.25</td>
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<td>35.76</td>
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<td>4.62</td>
<td>0.8</td>
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<tr>
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<td>34.91</td>
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<td>0.9</td>
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<tr>
<td>0.49378</td>
<td>31.8</td>
<td>103</td>
<td>29.82</td>
<td>11.57</td>
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<td>0.9</td>
<td>2.84</td>
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<td>67</td>
<td>24.19</td>
<td>13.70</td>
<td>5.63</td>
<td>1.0</td>
<td>2.84</td>
<td>0.009</td>
</tr>
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</table>

In the solution, allowing a direct comparison of the influence of NaClO₄ on the permittivity of the formamides.

The breakdown of the NMF permittivity to about 50% of εₛ(0) at a molar ratio of 5:100 shows that the structure of NMF is strongly affected by ion-solvent interactions. This behaviour is similar to methanol solutions [23, 24] and suggests that the average length of the hydrogen-bonded chains of solvent molecules is reduced. The static permittivity of DMF is much less affected, and at least at low concentrations the behaviour is comparable to NaClO₄ solutions of
Fig. 2. Relative change $\Delta \varepsilon_r / \varepsilon_r(0)$ of the solvent permittivity, $\varepsilon_r(c)$, as a function of the molar ratio $c/c_s$ of NaClO$_4$ to solvent in the solution at 25°C for 1: FA, 2: NMF, and 3: DMF.

Table 5. Parameters $\delta_\varepsilon$ and $\beta_\varepsilon$ of (3) and solvation numbers $Z_{IB}^\varepsilon$ according to (4) without ($\xi = 0$) and with correction for kinetic depolarization under stick or slip hydrodynamic boundary conditions.

<table>
<thead>
<tr>
<th></th>
<th>$\delta_\varepsilon$</th>
<th>$\beta_\varepsilon$</th>
<th>$Z_{IB}^\varepsilon$</th>
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<tr>
<td></td>
<td>$\text{dm}^3 \text{mol}^{-1}$</td>
<td>$\text{dm}^6 \text{mol}^{-2}$</td>
<td>stick</td>
</tr>
<tr>
<td>FA</td>
<td>29 ± 2</td>
<td>5 ± 2</td>
<td>5.7 ± 0.5</td>
</tr>
<tr>
<td>NMF</td>
<td>155 ± 3</td>
<td>60 ± 3</td>
<td>13.7 ± 0.3</td>
</tr>
<tr>
<td>DMF</td>
<td>17.7 ± 0.6</td>
<td>4.8 ± 0.7</td>
<td>5.9 ± 0.2</td>
</tr>
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</table>

Acetonitrile and propylene carbonate [23], solvents with interactions also dominated by dipolar forces. Interestingly the behaviour of FA is very similar to DMF. Here the lack of appropriate data prevents a comparison with solvents of related H-bond structure, like water or diols.

It is commonly assumed that the experimentally accessible dielectric decrement, $\delta_\varepsilon = \delta_\varepsilon^e + \delta_\varepsilon^d$ is the sum of an equilibrium contribution, $\delta_\varepsilon^e$, comprising irrotational bonding of a number of $Z_{IB}^\varepsilon$ solvent molecules in the field of the ions and volume effects, and of a dynamic contribution arising from kinetic depolarization, $\delta_\varepsilon^d$ [12]. Taking the initial slope $a_1$ of the solution density in the molarity scale, and $M_s$ and $M_{El}$ as the molar masses of solvent and electrolyte to express the volume effect yields

$$Z_{IB}^\varepsilon = \delta_\varepsilon^e L c_s(0) + \frac{a_1 - M_{El}}{M_s}, \quad (4)$$

where

$$L = \frac{2 e_x^2(0) + e_x^2(0)}{e_x(0)[e_x(0) - e_\infty(0)][2 e_x(0) + e_\infty(0)]} \quad (5)$$

is defined by the dielectric properties of the neat solvent (concentration $c_s(0)$). $Z_{IB}^\varepsilon$ can be compared with solvation numbers from other methods. However, it must be noted that this effective number of solvent dipoles, fixed per equivalent of electrolyte, is a measure for ion-solvent interactions and hence not necessarily equivalent to the geometry defined coordination numbers of the ions.

The correction for kinetic depolarization, $\delta_\varepsilon^d$, available from the initial slope of conductance vs. concentration,

$$\delta_\varepsilon^d = \xi \lim_{c \to 0} \left( \frac{\partial \varepsilon}{\partial c} \right)_T$$

with the depolarization factor $\xi$ available from theory is still a matter of discussion. The possible limits are given by Chandra et al. [25] suggesting $\xi = 0$, and by the continuum model of Hubbard et al. [26] yielding

$$\xi = p \cdot \frac{\varepsilon_x(0) - \varepsilon_\infty(0)}{\varepsilon_x(0)} \cdot \tau_s(0) / \varepsilon_0. \quad (7)$$

In (7) the parameter $p$ characterizes ion transport under stick ($p = 1$) or slip ($p = 2/3$) hydrodynamic boundary conditions.

Columns 4–6 of Table 5 summarize the corresponding $Z_{IB}^\varepsilon$ numbers obtained from the experimental decrements $\delta_\varepsilon$. For FA and DMF the results are in the range expected for solvents where anion solvation is weak [27] and cation solvation is restricted to the first solvation shell. The considerably larger values obtained for NMF, which compare with $Z_{IB}^\varepsilon$-data obtained for methanol solutions ($Z_{IB}^\varepsilon = 7.3$ [23]), show that the influence of Na$^+$ on the NMF structure is not restricted to the first solvation shell. Although hydrogen bonding between ClO$_4^-$ and the solvent molecules may also contribute to $Z_{IB}^\varepsilon$, the probable reason for the large values is an Na$^+$-induced reduction of the average NMF chain length, which is also inferred from $\tau_s(0)$ and the concentration dependence of the s2 process, see below. Comparison of $Z_{IB}^\varepsilon$ with the scarce solvation numbers from the literature is not helpful for a decision on the magnitude of the kinetic depolarization correction $\delta_\varepsilon^d$. In his review on solvation in non-aqueous solutions Ohtaki quotes Na$^+$ solvation numbers $n_+$, determined by transference number measurements, of $n_+ = 4$ for FA, $n_+ = 2.6$ for
NMF, and values of 3.0 and 3.3 for DMF [28]. James et al. [29] deduce \( n_+ \) (DMF) = 3.4 from Raman spectra whereas Sacco et al. [30] quote \( n_+ \) (DMF) = 6 in an NMR study. For the homologous solvent \( \text{N,N-dimethylacetamide} \), \( n_+ \) (DMA) = 6 for \( \text{Li}^+ \) and \( n_+ \) (DMA) = 4 for \( \text{Na}^+ \) are deduced from infrared studies [31]. Comparison of these data with the results of Table 5 at least suggests that in DMF, but probably also in FA, \( \text{Na}^+ \)-solute interactions are strong, but restricted to the first solvation shell.

### 3.3. Relaxation Time \( \tau_{s_1} \)

For a dispersion step \( j \), where dielectric relaxation originates from the diffusive reorientation of the molecular dipole moment \( \mu_j \), the molecular relaxation time, \( \tau_j \), is related to the bulk viscosity \( \eta \) via the extended Stokes-Einstein-Debye equation

\[
\tau_j = \frac{3 V_r}{k_B T \eta},
\]

where the effective volume of rotation, \( V_r = V_m f_\perp C \), is determined by the molecular volume of the rotor, \( V_m \), its deviation from spherical shape taken into account by \( f_\perp \), and by the parameter \( C \) (\( C = 1 \) for stick boundary conditions) coupling the frictional force felt by the rotating particle to \( \eta \) [32]. \( \tau_j \) can be estimated from the experimental relaxation time \( \tau_j \) as

\[
\tau_j = \frac{2 \varepsilon_j + \varepsilon_\infty \tau_j}{3 \varepsilon_j}.
\]

Figure 3 shows the relative change of relaxation time, \( \Delta \tau_{s_1}(c)/\tau_{s_1}(0) = (\tau_{s_1}(c) - \tau_{s_1}(0))/\tau_{s_1}(0) \), of the s1-process as a function of \( c/c_s \). Having in mind that \( \eta \) increases with electrolyte concentration for all three solvents, cf. Table 1, it is obvious for NMF (curve 2) that the dominating dispersion step does not originate from the rotational diffusion of single molecules. Indeed, the concentration dependence of \( \tau_{s_1} \) resembles that of methanol in \( \text{NaClO}_4 \) solutions [23]. For the alcohol it was argued that the slow relaxation process probes the probability that different hydrogen-bonded chains "react", thus lead to a large change of the overall dipole moment [33]. Thus, the increase of the relaxation rate \( \tau_{s_1}^{-1} \) with electrolyte concentration suggests that beyond ion solvation \( \text{NaClO}_4 \) increases the number of NMF chains by reducing their average length in accordance with the interpretation of \( \varepsilon_s(c) \).

For DMF \( \tau_{s_1}^{-1} \) increases linearly with viscosity, see curve 1 of Fig. 4, indicating diffusive reorientation of the solvent dipoles. The slope of \( \tau_{s_1}^{-1} = f(\eta) \), (8), yields as the experimental volume of rotation \( V_r^{\text{ex}} = (3.57 \pm 0.05) \cdot 10^{-30} \text{m}^3 \), a much smaller value than the molecular volume of \( V_m(\text{DMF}) = 144 \cdot 10^{-30} \text{m}^3 \) estimated from intramolecular distances [9] and van der Waals radii [35], whereas \( V_r(0) = 12.5 \cdot 10^{-30} \text{m}^3 \) is obtained when the data of neat DMF (c = 0) are inserted into (8). A separation of \( f_\perp \) and \( C \) is not straightforward since DMF is neither a spheroid nor is the dipole vector coinciding with one
of axes of inertia. However, the ratio $V_r(0)/V_m \approx 0.09$ suggests that the rotational motion of the solvent molecules is only weakly coupled to shear stress. Moreover, from $V_{sa}^s/V_r(0) \approx 0.29$ it can be deduced that the electrolyte which creates a marked viscosity increase has only a limited influence on the reorientation of the solvent molecules in the bulk. Hence solution properties seem to be dominated by the large particles formed of Na$^+$-ions surrounded by one solvation shell which are immersed in the only weakly perturbed solvent, a behaviour also observed for solutions in acetonitrile [34].

Formamide, $V_m = 50 \cdot 10^{-30} \text{m}^3$ according to the data of [35, 36], also exhibits an increase of $\tau_{s1}$ with increasing $c/c_s$, see curve 1 of Figure 3. Compared to DMF the values of $\tau_{s1}$ and $\eta$ are roughly increased by a factor of 3 due to the H-bonding network which determines the liquid structure [7]. If (8) is tentatively applied – bearing in mind that the classical definition of rotational diffusion does not apply – the data at $c = 0$ yield $V_r(0) = 10.7 \cdot 10^{-30} \text{m}^3$ and hence $V_r(0)/V_m \approx 0.21$, reflecting the stronger coupling of dipole reorientation to the environment through hydrogen bonding. However, the influence of ion-solvent interactions on $\tau_{s1}$, expressed by $V_{sa}^s = (0.55 \pm 0.03) \cdot 10^{-30} \text{m}^3$ and $V_{sa}^s/V_r(0) \approx 0.05$, is very weak. This is also reflected by the only small increase of the relaxation-time distribution parameter $\tau_{s1}$. Probably $\tau_{s1}$ primarily reflects the formation kinetics of mobile, i.e. non- or single-hydrogen bonded FA molecules from the network in a way similar to aqueous solutions [37], a process only weakly disturbed by the electrolyte in the studied concentration range $c/c_s < 4:100$.

3.4. The $s_2$ Process of NMF

Comparable to methanol [33], NMF exhibits a small amplitude process (only 0.8% of the total dispersion $\varepsilon - \varepsilon_{\infty}$ at $c = 0$) with a relaxation time $\tau_{s2} \approx 8 \text{ps}$, a value in the range expected for the reorientation of a single molecule. Hence an interpretation of the $s_2$ process in terms of the reorientation of "mobile" NMF molecules seems appropriate. Indeed a plot of $\tau_{s2}$ vs. viscosity, curve 2 of Fig. 4, is linear, and its slope yields an experimental volume of rotation, $V_{r}^{a1} = (2.7 \pm 0.4) \cdot 10^{-30} \text{m}^3$. From the data of [8, 35] a molecular volume of $V_m = 80 \cdot 10^{-30} \text{m}^3$ can be estimated, whereas the data of neat NMF inserted into (8) yield $V_r(0) = 10.7 \cdot 10^{-30} \text{m}^3$, hence $V_r(0)/V_m \approx 0.07$ and $V_{sa}^s/V_r(0) \approx 0.47$ are obtained. Both ratios are comparable to those of DMF and hence suggest that the – more or less diffusive – reorientation of single molecules is probed. As for methanol, this probably incorporates monomers together with NMF molecules at chain ends involved in a single hydrogen bond.

For process $j$ of a multistep relaxation the concentration $c_j$ of the relaxing species can be inferred from the dispersion amplitude $A_j = \varepsilon_j - \varepsilon_{\infty}$ and its dipole moment $\mu_j$ with the help of Cavell’s equation [38]

$$c_j = \frac{2 \varepsilon_0 + 1}{3 \varepsilon_0} \cdot \frac{3 k_B T \varepsilon_0}{N_A} \cdot \frac{(1 - f_j z) \mu_j^2}{\Delta_j} \cdot A_j. \quad (10)$$

In (10) $z_j$ is the polarizability of the dipole, and the reaction field factor $f_j$ is accessible from the expressions of Scholte [39].

Taking $\mu_{s2} = \mu(\text{NMF}) = 12.7 \cdot 10^{-30} \text{Cm}$ and $\alpha(\text{NMF}) = 7.69 \cdot 10^{-40} \text{C}^2 \text{m}^2 \text{J}^{-1}$ [40] the relative concentrations $c_{s2}/c_s$ of Fig. 5 are obtained for the data $A_{s2} = \varepsilon_{s2} - \varepsilon_{s3}$ of Table 3. Except for the diffraction study of Neuefeind et al. [10], who claim that only about 50% of the molecules are hydrogen bonded, to our knowledge no determination of the concentration of monomers and chain ends in liquid NMF is available from the literature. But according to far-infrared spectra, hydrogen bonding seems to predominate even at high dilution in tetrachloromethane [21], and similar values for the monomer fraction are obtained for methanol from various simulation studies, see [33] for references. Therefore, a 3% fraction of mobile NMF molecules in the neat liquid seems plausible. If we assume that the $s_2$ process is mainly due to the...
reorientation of molecules at chain ends the linear increase of slope $0.48 \pm 0.04$ exhibited by $\varepsilon_{s2}/\varepsilon_s$ vs. relative electrolyte concentration, $c/c_s$, suggests a solute induced increase of the number of hydrogen-bonded NMF chains at the cost of a reduced average length. Hence the conclusions obtained from $\varepsilon_s(c)$ and $\tau_{s1}(c)$ are corroborated.

3.5. The High-frequency Process

All formamides exhibit a fast relaxation process, $s_2$ for FA and DMF, $s_3$ for NMF, of small amplitude and relaxation time around 1 ps – just like water and the lower alcohols [23], see Tables 2–4. Originally it was assumed that this process might monitor the kinetics of H-bond formation for the amphiprotic hydroxylic (water, alcohols) and protophilic H-bond donor (FA, NMF) solvents. However, neither the results from a dielectric study of methanol-tetrachloromethane mixtures [33], nor from an investigation of aqueous electrolytes [37] support the assumption that the high frequency process is a direct measure of the hydrogen-bond life time. For the aprotic protophilic solvents DMF and N,N-dimethylacetamide the hindered intramolecular rotation of the dimethylamino group around the C–N bond is also not a convincing reason for the high frequency mode because of its high activation energy, $\Delta G^* = 87.5$ kJ mol$^{-1}$ [41], in contrast to earlier discussions [16].

FA, NMF, and DMF are asymmetric rotors with the dipole vector not coinciding with an axis of inertia, Fig. 6, so that three relaxation times should be expected. A direct scaling of these $\tau$-values with the moments of inertia, $I_j$, cannot be expected since hydrodynamic interactions following (8) as well as specific interactions through hydrogen bonding predominate. However, it is obvious from Table 6 that for all formamides $I_z$ is considerably smaller than the other moments of inertia, making rotation around the $z$-axis the possible origin for the fast relaxation process. This is supported by the isotope effect on the two relaxation times of the polarizability tensor observed by Chang and Castner in their OH-D-RIKES study of FA, DMF, and their deuterated homologues [42].

Further support comes from $^{13}$C NMR relaxation. With this technique Konrat and Sterk [43] recently determined the individual diffusion constants for re-orientation of DMF around the axes of inertia and obtained for rotation around the $z$- and $y$-axis the correlation times $\tau_z \approx 1.3$ ps and $\tau_y \approx 12.6$ ps, which are comparable to $\tau_{s2} = 0.74$ ps and $\tau_{s1} = 10.36$ ps, respectively. The small component of $\mu$ normal to $z$ might account for the small amplitude $\varepsilon_{s2} - \varepsilon_{s0}$.

In [43] also the rotation of the DMF molecule around the $x$-axis normal to the molecular plane is observed, $\tau_x \approx 85$ ps. Such a process is not seen in the complex permittivity spectrum of DMF inspite of the large component of $\mu$ and a ratio $I_x/I_y$ which should be sufficient to distinguish the corresponding relaxation times. Possibly this arises from the stacked parallel plate arrangement with antiparallel dipole moments deduced by Yashonat and Rao from their molecular dynamics investigation [44].

For FA and NMF $I_x/I_y$ is closer to unity and hydrogen bonding complicates the relaxation behaviour. Therefore, a possible splitting of the $s_1$ process of FA and of the $s_2$ process of NMF cannot be resolved.

3.6. Ion-pair Relaxation in DMF

In addition to the solvent relaxation processes $s_1$ and $s_2$, the electrolyte solutions of DMF exhibit an additional low-frequency relaxation process centered around 1.5 GHz which is typical for the relaxation of dipolar ion pairs formed by the electrolyte [12]. It is
possible to determine the concentration of ion pairs, $c_{\text{IP}}$, with the help of (10) from the experimental dispersion amplitude $A_{\text{IP}} = \varepsilon - \varepsilon_s$. The ion-pair dipole moment, $\mu_{\text{IP}}$, can be calculated as a function of charge separation $d = r_+ + r_- + 2kr_-$ [37]. From $c_{\text{IP}}$ the association constants $K_A$ of the model ion-pairs for contact (CIP, $k = 0$), solvent-shared (SSIP, $k = 1$), and solvent-separated (2SSIP, $k = 2$) species can be estimated with the extrapolation

$$K_A = \lim_{c \to 0} \frac{c_{\text{IP}}}{(c - c_{\text{IP}})^2}$$  \hspace{1cm} (11)

Taking the ionic radii $r_+ = 98$ pm, $r_- = 240$ pm, and polarizabilities $\chi_+ = 0.20 \cdot 10^{-40}$ C² m² J⁻¹, $\chi_- = 5.59 \cdot 10^{-40}$ C² m² J⁻¹ of Na⁺ and ClO₄⁻, respectively, [45] and the solvent data $r_s = 330$ pm [46] and $\chi_s = 8.77 \cdot 10^{-40}$ C² m² J⁻¹ [47] the results of Table 7 are obtained. Comparison of the $K_A$-values with the conductimetrically determined $K_A = 3.2$ dm³ mol⁻¹ [46] reveals the solvent-shared ion pair, $k = 1$, as the relaxing species.

This observation is corroborated by the molecular relaxation time of the ion pair, $\tau_{\text{IP}}$, determined from the experimental $\tau_{\text{IP}}$-data with the help of the expression

$$\tau_{\text{IP}}^{-1} = (\tau_{\text{IP}})^{-1} + k_{21} + 2k_{12}(c - c_{\text{IP}}),$$  \hspace{1cm} (12)

where $k_{12}$ and $k_{21} = k_{12}/K_A$ are the rate constants of ion-pair formation and decomposition [48]. From the intercept of (12) the value of $\tau_{\text{IP}} = 260 \pm 30$ ps is obtained, which is between the results of (8) calculated for the geometric parameters of SSIP under the assumption of stick, $\tau_{\text{IP}}(\text{stick}) = 420$ ps, and slip boundary conditions, $\tau_{\text{IP}} = (\text{slip}) = 150$ ps. For the CIP and 2SSIP models (8) yields unrealistic results.

The rate constants of ion-pair formation, $k_{12} = (4.7 \pm 0.2) \cdot 10^9$ dm³ mol⁻¹ s⁻¹, and decay, $k_{21} = (1.5 \pm 0.2) \cdot 10^9$ s⁻¹ (corresponding to an ion-pair life time of $ln 2/k_{21} = 460$ ps), are in the range expected for diffusion controlled reactions [49]. Therefore, unlike to other systems, cf. [34, 48], desolvation is not an important step in ion-pair formation.

The synopsis of these results with the information from the solvent relaxation processes suggests that the solution properties of NaClO₄/DMF are dominated by Na⁺-ions with strong ion-solvent interactions restricted to the first solvation shell. These form short-lived complexes on encounter with the essentially unsolvated ClO₄⁻-anions but only weakly affect structure and dynamics of the bulk solvent.

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Table 7. Dipole moments of the model ion pairs CIP, SSIP, and 2SSIP, and association constants $K_A$ from dispersion amplitudes (this work) and from conductance data, [46].

<table>
<thead>
<tr>
<th>k</th>
<th>$\mu_{\text{IP}}$ (10⁻³⁰ C m)</th>
<th>$K_A$ (dm³ mol⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CIP</td>
<td>0 46.7</td>
<td>70 ± 2</td>
</tr>
<tr>
<td>SSIP</td>
<td>1 159</td>
<td>1.9 ± 1.3</td>
</tr>
<tr>
<td>2SSIP</td>
<td>2 265</td>
<td>0.6 ± 1.3</td>
</tr>
</tbody>
</table>