Fission of Heavy Elements Induced by Medium High Energy Protons

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Dedicated to Professor Dr. W. GENTNER on the occasion of his 60th birthday

Fissionability, mass distribution, charge dispersion and distribution, and neutron emission for fission induced in heavy targets (uranium) by protons with a few hundred MeV kinetic energy are presented and phenomenologically discussed. The results are interpreted in order to arrive at the reaction mechanisms in medium high energy induced fission.

In this paper is presented a discussion of fission induced in heavy elements (uranium) by protons with kinetic energies below about 400 MeV with the main emphasis on fission with protons of a few hundred MeV energy*. Thus, reactions where meson interference becomes of any importance are not considered. Even if fission is the main reaction in heavy nuclei this can not be discussed without consideration of the cascade-evaporation process generally considered to take place at high energy interactions with complex nuclei.

As described by the SERBER model these reactions start with a fast nucleonic cascade (time scale $\sim 10^{-22}$ sec) in the target nuclei knocking out neutrons and protons and leading to a variety of product nuclei — each with broad distribution of excitation energies — cascade residuals.

The subsequent deexcitation of the cascade residuals takes place by successive evaporations of nucleons (time scale $\gg 10^{-20}$ sec), each with a few MeV of kinetic energy (in heavy targets mainly neutrons) and leaving behind a complex mixture of reaction products — spallation products. Both steps of this model have been treated by the Monte Carlo method$^4,5$.

The results of the calculations are in good agreement with the experimental data for the light particles knocked out and emitted in the two steps at energies of interest for the present study.

The spectrum and yields of the spallation products from heavy targets as estimated according to this model are, however, upper limits, because in targets such as trans lead elements an additional difficulty enters the spallation picture. This is caused by a severe competition from fission during each stage of the evaporation chain, which lowers the yields of the spallation products. Such interference has also been treated by Monte Carlo methods$^6,7$.

Thus high energy induced reactions in heavy target nuclei will result in a very large variety of

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1. R. SERBER, Phys. Rev. 72, 1114 [1947].
heavy primary reaction products as result of the nucleonic cascade and the evaporation-fission competition. Furthermore, the primary fission fragments will de-excite by neutron evaporation, and the number of evaporated neutrons may in extreme cases be rather large (Fig. 1).

Even if spallation and fission each results in a complex mixture of products covering broad regions in the “Table of Nuclides”, the “region of interest” for the different processes can be distinguished to some extent, depending on the energy of the bombarding particle. For uranium and bombarding energies below about 400 MeV the fission region is clearly defined to the mass number region 60 – 160. Results to be presented in this paper are mainly obtained through radiochemical analysis, but results from ionization chamber measurements and loaded emulsion studies are included to some extent as a supplement to the radiochemical studies.

Fissionability

According to the Monte Carlo calculations 2,3 the total inelastic cross section $\sigma_T$ should be nearly independent of energy above 100 MeV, in agreement with experimental data 8. Due, however, to nuclear transparency 2 this cross-section is expected to be slightly below the geometrical one, $\sigma_{\text{geom}}$, for heavy elements at these energies, but to a first approximation and within the experimental errors not far from $\sigma_{\text{geom}}$.

The fission cross sections at different energies and targets as measured by chemical and by physical methods scatter somewhat, but with a few exceptions these are in agreement within 20\% or less 9. As pointed out byPerfilov 10 and by Pappas 11, using average values and total inelastic cross sections, the fissionability for elements tantalum and heavier, defined as $\sigma_f/\sigma_T$, increases with proton energy ultimately level off or for trans lead elements reaches a flat broad maximum whereafter it decreases steadily. The decrease may primarily be ascribed to increasing interference of other reactions caused by meson production. This becomes of particular importance in heavy elements where many of the pions produced have a chance to be reabsorbed within the mother nucleus 12.

Thus the maximum contribution from fission is found at bombarding energies 100 to 300 MeV for thorium and uranium, but at considerably higher energies, 400 – 800 MeV, for bismuth. Elements thorium and heavier belong to the highly fissionable ones where fission predominates over spallation and other reactions ($\sigma_f/\sigma_T = 0.5 – 1$). These nuclei are all characterized by a low fission threshold, in the vicinity of neutron binding energies ($\sim 5$ MeV). In the lead region fission is less probable ($\sigma_f/\sigma_T = 0.05 – 0.1$) and characterized by a high fission threshold, higher than neutron binding energies. For still lighter elements the fission thresholds are considerably higher than neutron binding energies and amount to tens of MeV, and fission should become very unlikely compared to spallation for these elements.

The dependence of $\sigma_f/\sigma_T$ on nuclear size does not seem to be as strong in high energy induced fission as in fission induced by low energy (few MeV) bombardments. As, however, in the latter case the former can be represented by a $Z^2/A$ dependence 10,11 and the maxima in the $\sigma_f/\sigma_T$ versus energy curves are, according toPerfilov 10, given by

$$(\sigma_f/\sigma_T)_{\text{max}} \propto \exp\left[0.682 \left(\frac{Z^2}{A} - 36.25\right)\right],$$

with $\sigma_T = 1.26 A^{0.19 - 0.41} \times 10^{-2}$ b.

The maximum fissionability of uranium occurs in the energy region 100 – 300 MeV and is about 80\%. Thus the studies by the author and his collaborators on fission of uranium with 170 MeV protons 13–19 fall in the middle of the maximum fissionability of uranium. The latest fission cross section measurements give (1.4 ± 0.1) b at 170 MeV measured.

radiochemically, 1.37 b at 150 MeV as determined by ionization chamber, and (1.46 ± 0.06) b at 280 MeV based on fragment track techniques.

The fissionability for a given nucleus at a given excitation energy will increase when its angular momentum is increased. Thus the fissionability in high energy proton bombardments should be expected to increase in those cases where large angular momenta are involved, but no separation of results from low and high angular momentum proton interactions have yet been made. The effect of high angular momenta on fissionability is preferentially studied by using complex projectiles.

Mass distribution

For highly fissionable nuclei the valley in the double peaked mass yield curve characteristic for low energy induced fission of these elements is gradually filled in when the bombarding energy increases towards 50 – 100 MeV. From the relatively few data available the mass yield curves above 100 MeV bombarding energy have been assumed to be single peaked with a flat maximum extending over 30 to 40 mass numbers and reflection symmetric except for the extreme light and heavy masses (Fig. 2.74 in ref. 24). But as first indicated by Rudstam and Pappas in an analytical treatment of 170 MeV proton induced fission based on a model of two different modes of fission: symmetric and asymmetric, the mass distribution should be neither single peaked nor reflection symmetric. This has recently been verified experimentally by Pappas and Hagebo, and their mass yield curve is given in Fig. 2. At higher excitation energies only incomplete experimental information is available, thus similar details of the mass distribution above 200 MeV are not available.

The discrepancy between the yields at the wings and the reflected ones increases with energy. This is mainly due to a relative increase of the yields in the light wing, while the yields in the heavy wing are relatively more independent of energy. (Fig. 2.74 in ref. 24). By comparing crude mass yield distributions at various energies Friedlander shows (Fig. 3) that the “peak” of the distribution moves slowly towards lower mass numbers with increasing proton energy — from \( A \) about 118 at 100 MeV to \( A \) about 107 at 28 GeV. This trend can be ascribed to a broadening of the distribution of cascade residuals and to higher average deposition energies.

That the mass yield curves in high energy induced fission show both symmetric and asymmetric trends do not necessarily involve that these curves are results of the two modes of fission: symmetric and asymmetric. The agreement between the observed distribution and that expected by the model used by Rudstam and Pappas may be fortuitous. An asymmetry in the curve might also be a sum of symmetric mass splitting of fissioning nuclei with large

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23 Reflection symmetric, i.e. reflection of yields around a most probable mass.
Fig. 3. Mass yield curves for uranium bombarded by protons of various energies, taken from ref. 25. a) 100 MeV \(^{26}\), b) 170 MeV \(^{17}\), c) 2.9 GeV \(^{25}\), d) 28 GeV \(^{25}\).

Fig. 4. Fragment range distributions from fission of uranium at different excitation energies, taken from ref. 27.

differences in mass number and in varying abundance and excitation energy. Thus the contribution from asymmetric splitting of nuclei can not be settled from studies of mass yield curves alone.

However, studies of charge dispersion and distribution in 170 MeV proton induced fission of uranium point towards a real contribution from the asymmetric fission mode at least in the heavy wing\(^{16}\). A support in this direction is also given by SHAMOV and LOZHIN\(^{27}\) in their studies of ranges of fission fragments in nuclear emulsion (Fig. 4). These authors show that fission of uranium is most symmetric at excitation energy 60 — 100 MeV of the fissioning nucleus. However, the amount of highly asymmetric division at this energy (with range of light fragment/range of heavy fragment larger than 1.4 to 1.5) is about the same as in thermal fission. (Their observation that at higher energies the contribution from asymmetric fission increases again is hard to explain.)

The assumption, therefore, made by RUDSTAM and PAPPAS\(^{17}\) seems to be confirmed: Any fission nucleus at any energy can have two different modes of fission (symmetric or asymmetric) with relative probabilities depending systematically on charge and mass number and excitation energy. Those dependencies can be evaluated from experimental data from low energy fission.

As shown by LINDNER and TURKEVICH\(^{7}\), when comparing their results from Monte Carlo calculations with experimental information, the fission — evaporation competition \(\Gamma_f/\Gamma_n\) in the second step of the SERBER model seems to be a function of nuclear type only and not very much on excitation energy below about 100 MeV. Thus it is most appropriate to use the results in ref. 17, which are based on energy independent fission parameter

\[
G = \Gamma_f/(\Gamma_f + \Gamma_n + \Gamma_r).
\]

One would then expect that the asymmetric fission mode would vanish at some excitation energy in the 100 — 200 MeV region. (Fig. 2 in ref. 17). Thus the mass yield curve will probably keep its general “structure” until the meson influence is reached.

**Charge Dispersion and Distribution\(^{28}\)**

In thermal and low energy induced fission of uranium a large amount of information is available concerning charge dispersion and distribution.


28 The nomenclature proposed by FRIEDLANDER\(^{25}\) will be used in this discussion, i. e.

\[\text{Charge dispersion} = \text{distribution of independent fission yields among the isobars at a given mass number},\]

\[\text{Charge distribution} = \text{the manner in which the nuclear charge divides itself between the two fragments in the fission act}.\]
The previous heavy support\textsuperscript{29} (radiochemical) to the empirical equal charge displacement rule (ECD) by GLENDENIN, CORYELL and EDWARDS\textsuperscript{30} in favour of other postulates for the division of nuclear charge in fission — the charge distribution, has been enlarged by X-ray identification of charges\textsuperscript{31}. In medium and high energy induced fission of bismuth the unchanged charge distribution rule (UCD), proposed by GOECKERMANN and PERLMAN\textsuperscript{32}, accounts for the experimental observations. Thus it is common to assume that ECD and UCD belong to the asymmetric and the symmetric fission modes, respectively.

In medium high energy induced fission of elements thorium and heavier there have been different opinions concerning the charge division. The detailed study of fission of uranium induced by 170 MeV protons\textsuperscript{16–19} has, however, disclosed that both the above hypotheses seem to find experimental supports.

The largest contribution from ECD is found in the heavy wing\textsuperscript{16}, showing the importance of low energy modes of fission (asymmetric) where the fissioning nuclei still keep some “memory” of shell structure. The light wing, however, follows more the UCD trend, as a result of high energy deposition events\textsuperscript{18}. This applies to both the neutron to proton ratios of the most probable primary charge $Z_p$ and to the widths of the charge dispersion curves. Thus both fission modes contribute, and a mass dependent mixture of these charge distribution rules seems to be present. The mass dependence of these is therefore not quantitatively predicted by RUDSTAM and PAPPAS\textsuperscript{17}. In general the experimental neutron to proton ratios, $N/Z$ values, fluctuate between the limits given by the two rules. This is in qualitative agreement with what would be expected when the fissioning nuclei have a broad excitation energy spectrum.

Both charge dispersion curves observed are narrow “thermal like” gaussian curves. The width at half-maximum which is about 2.2 units in the light mass region increases slightly to 2.8 for the medium region and decreases to 2.2 in the heavy region.

Thus the previous explanation\textsuperscript{16, 33} of a broad isotopic distribution curve for iodine\textsuperscript{14} to mean a very broad charge dispersion curve in this region (width $\sim 4$ charge units) is not completely justified by the more detailed investigation\textsuperscript{19}. There is, however, still a significant difference ($25 - 30\%$) in the widths of the charge dispersion curves for symmetric and asymmetric fission at 170 MeV. Thus the conclusion made by PAPPAS and ALSTAD in\textsuperscript{16}, partly based on work by PATE et al.\textsuperscript{33} that the width of the charge distribution curve in symmetric fission increases with increasing bombarding energy while that for asymmetric fission is independent of energy, is still valid. As shown by FRIEDLANDER\textsuperscript{25}, the yield versus $N/Z$ curves for $A = 131$\textsuperscript{34} are double peaked in the GeV region. The widths of the corresponding charge dispersion curves can be estimated to $\sim 4$ and $\sim 3$ charge units for the neutron deficient and neutron rich peak, respectively. The latter peak must be ascribed to symmetric fission and its width is as

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig5.png}
\caption{The neutron to proton ratio $N/Z_p$ for the most probable primary charge $Z_p$ versus product mass number. Mass yield curve from Fig. 2. Both for uranium fission induced by 170 MeV protons\textsuperscript{19}.}
\end{figure}


\textsuperscript{32} R. H. GOECKERMANN and I. PERLMAN, Phys. Rev. 76, 628 [1949].

expected by extrapolation from data at lower energies. The neutron deficient peak may indicate some type of a non fission contribution. The neutron to proton ratio $N/Z_p$ of the most probable fission products as function of mass number in 170 MeV proton induced fission of uranium has also been studied by Pappas and Hagebo. Their curve is reproduced in Fig. 5 on the mass yield, curve. The dip in the curve below the general trend (dotted) is in the same mass region as the symmetric peak in the mass yield curve. Thus one should conclude from position and $N/Z_p$ ratio that symmetric fission mode is caused by high energy deposition events.

Neutron emission

Correlation studies between fission fragments and neutrons in high energy induced fission are only available for protons with 150 MeV kinetic energy on uranium. Harding and co-workers report 13.1 ± 1.8 neutrons emitted, with only about 2.5 neutrons emitted post fission. The majority of the neutrons are most likely emitted from nuclei which after fission give products in the middle part of the mass yield curve. For fissioning nuclei giving products in the light wing however the radiochemical studies seem to indicate 1. a large post fission neutron emission from light primary fission fragments, but due to low yields these neutrons are difficult to distinguish in the neutron measurements, and 2. that light products may also be formed in fission of light uranium nuclei which have evaporated many neutrons before fission.

The number of emitted neutrons is directly related to the excitation energy of the nucleus terminating the cascade. Therefore the light products are mainly the result from very high energy deposition events ($\sim 15\%$ compound formation is expected). This conclusion is supported by a quite different approach - recoil studies of fission fragments from uranium bombarded with 150 MeV protons by Noshkin and Sugihara and with 450 MeV protons by Sugarman et al. Both these groups have shown that the excitation energies of residual nuclei leading to light fragments are about twice the energies of nuclei leading to heavy fragments.

A study of the number of pre-fission neutrons emitted versus mass number of the fission product is possible from the radiochemical yield measurements by Pappas and Hagebo. Their results are reproduced as curve A in Fig. 6 and the energy effect on the symmetric peak is also here very pronounced and supports the results from the charge distribution study (Fig. 5). One could therefore make the conclusion that the products concerned must be the result of events from the higher part of the excitation energy distribution of the nuclei terminating the cascade.

Fig. 6. Curve A: Pre fission emission of neutrons versus fission product mass number for fission of uranium with 170 MeV protons. Curve B: Cascade deposition energy for most probable primary charge $Z_p$ versus fission product mass number for fission of uranium with 450 MeV protons, taken from ref. 39.

The shape of curve A in Fig. 6 is in qualitative agreement with that of curve B. The latter gives the variation with mass number of the cascade deposition energy for the most probable charge in 450 MeV proton fission of uranium. This curve is determined by Sugarman et al. on the basis of recoil studies. That the horizontal part of curve B is displaced towards higher mass numbers is a result of the expected larger contribution from products from

Thus 2.5 neutrons are in general assumed to be emitted from the primary fission fragments in the following discussion.

higher deposition energy events. This curve gives directly the neutron emission curve for 450 MeV fission by using the left ordinate (~10 MeV separation and kinetic energy per neutron emitted).

The agreement obtained by two so different approaches as fission yield measurements and recoil studies is very encouraging and supports the validity of results obtained by either methods and the conclusions drawn in this paper.

Conclusion

The results of the present investigation are summarized schematically in Fig. 7, where the origin to the different parts of the mass yield curve in fission of uranium with 170 MeV protons is illustrated. At the bottom of the figure is drawn also schematically the gross distribution of deposition energy (taken from ref. 2). The small peak to the left represents the about 15% compound nucleus formation which takes place 2.

A number of interesting features is seen from this figure:

A) The asymmetric fission peaks are in general the result of the asymmetric fission mode which occurs at all excitation energies. The charge distribution will therefore follow more close the equal charge displacement rule (ECD) than the unchanged charge distribution rule (UCD).

B) The heavy wing is due to fission of heavier nuclei, i.e. to low or moderate energy deposition events (low energy fission). The light fragment from these events will be drawned under the light peak. In the heavy wing will the ECD rule be most pronounced.

C) The light wing is due to high deposition energy events, including compound nucleus formation. The heavy products from these events will be drawned under the heavy peak. In the light wing will the UCD rule be most pronounced.

D) The symmetric peak is due to events from the higher part of the deposition energy distribution and is in general the result of the symmetric fission mode. Thus the charge distribution will follow more closely the UCD than the ECD rule.

Thus fission of heavy elements induced by protons with about 200 MeV kinetic energy is not different in any essential way from fission induced by particles of a few tens of MeV kinetic energy. The maximum fissionability of uranium is reached at about 200 MeV bombarding energy. From then on other processes (or mechanisms) than fission start contributing.

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